

In[34]:= $k[x_] = 2 * x^3 / (x^2 - 1)$

Out[34]=
$$\frac{2x^3}{-1 + x^2}$$

In[35]:= $r[x_] = 2 * x^3 / ((1 + x^2)^2)$

Out[35]=
$$\frac{2x^3}{(1 + x^2)^2}$$

In[38]:= **Simplify[D[k[x], x]]**

Out[38]=
$$\frac{2x^2(-3 + x^2)}{(-1 + x^2)^2}$$

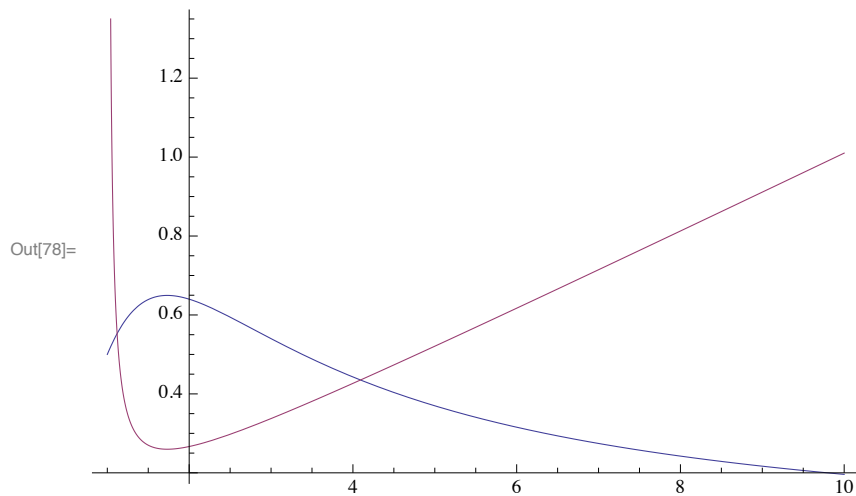
In[39]:= **Simplify[D[r[x], x]]**

Out[39]=
$$-\frac{2x^2(-3 + x^2)}{(1 + x^2)^3}$$

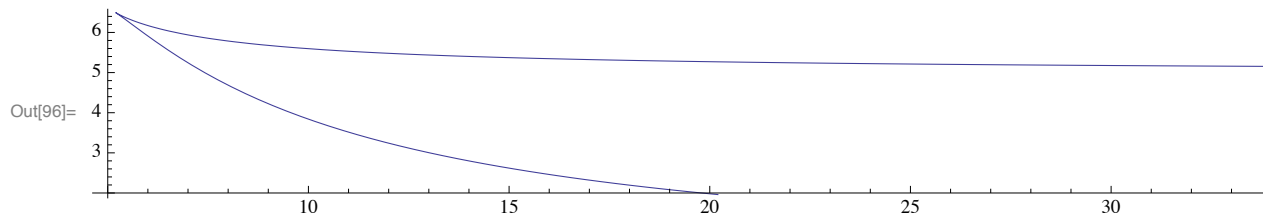
In[36]:= **Simplify[D[r[x], x] / D[k[x], x]]**

Out[36]=
$$-\frac{(-1 + x^2)^2}{(1 + x^2)^3}$$

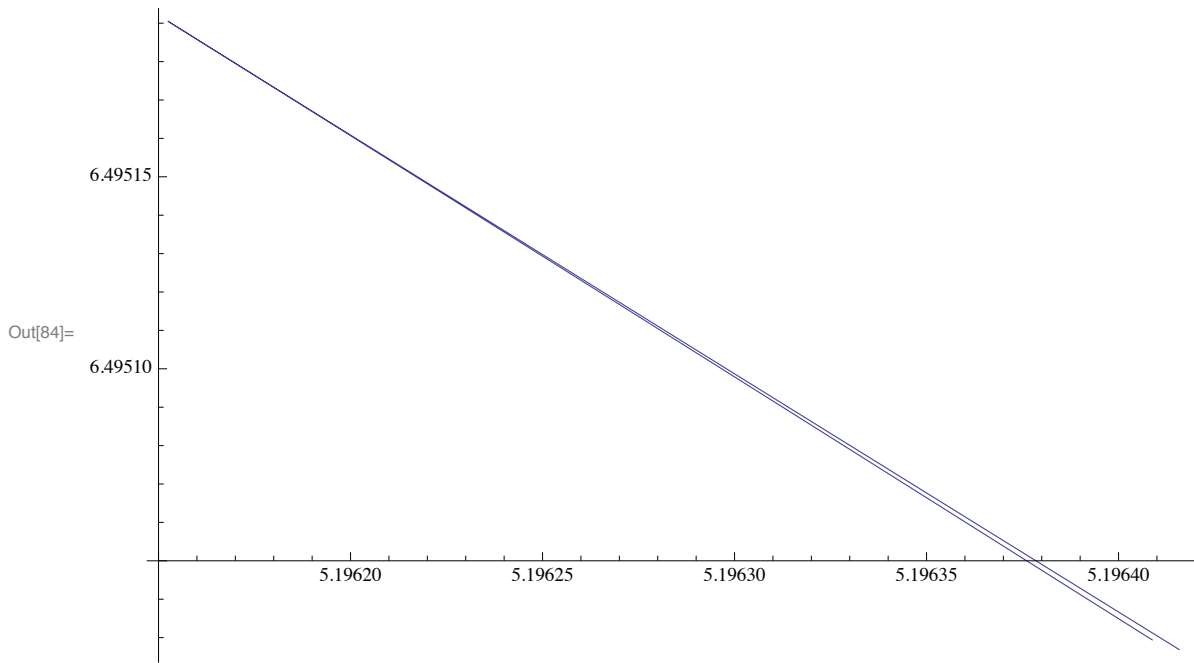
In[78]:= **Plot[{r[x], k[x] / 20}, {x, 1, 10}]**



In[96]:= **ParametricPlot[{k[x], 10 * r[x]}, {x, 1.01, 10}]**



In[84]:= **ParametricPlot**[{**k**[**x**], **10 * r**[**x**]}, {**x**, **Sqrt**[**3**] - **0.01**, **Sqrt**[**3**] + **0.01**}]



In[79]:= **k**[**Sqrt**[**3**]]

Out[79]= $3\sqrt{3}$

In[81]:= **N**[**k**[**Sqrt**[**3**]], **20**]

Out[81]= 5.1961524227066318806

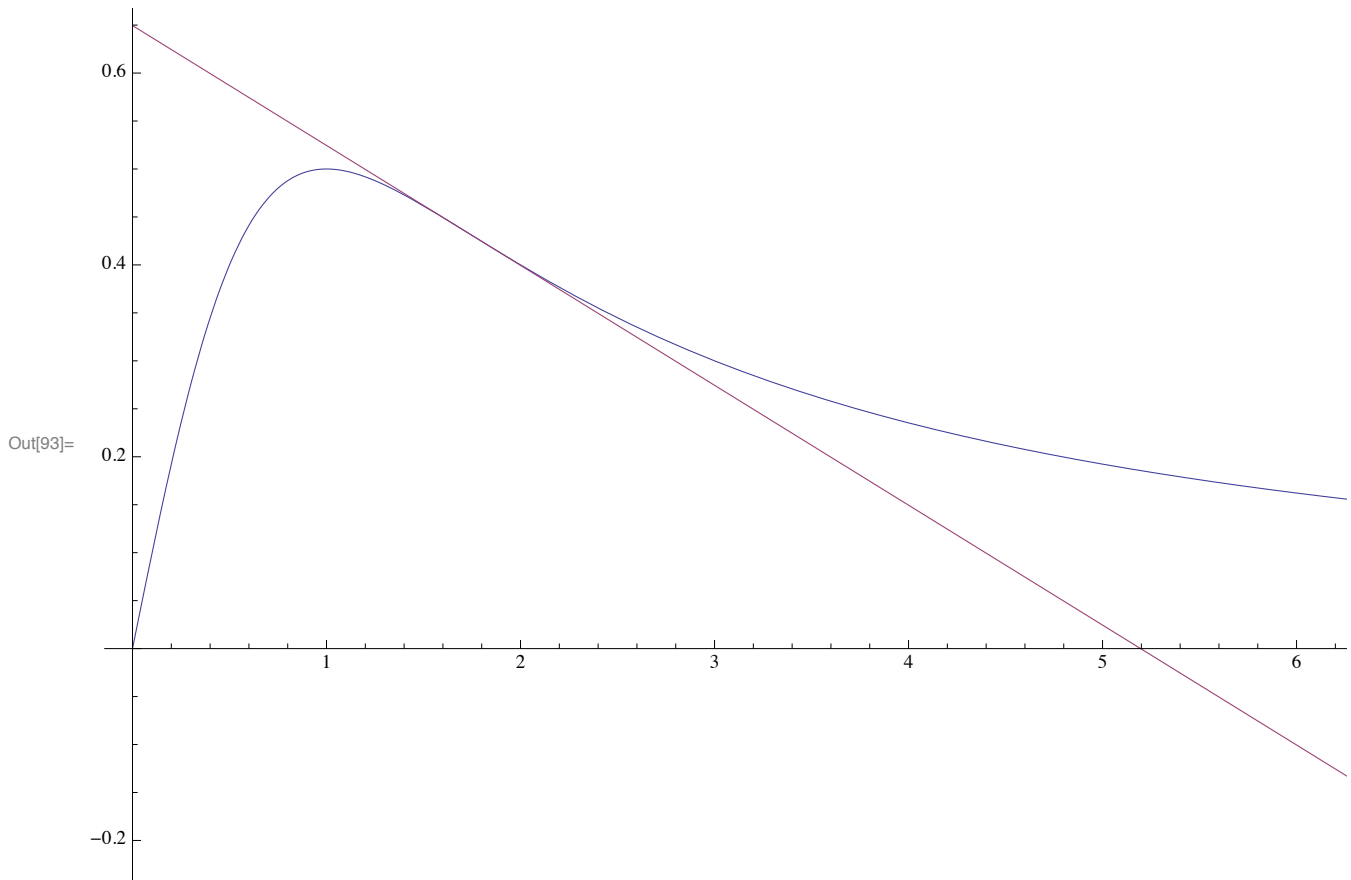
In[82]:= **r**[**Sqrt**[**3**]]

Out[82]= $\frac{3\sqrt{3}}{8}$

In[83]:= **N**[**r**[**Sqrt**[**3**]], **20**]

Out[83]= 0.64951905283832898507

In[93]:= **Plot**[{ $x / (x^2 + 1)$, $3 \sqrt{3} / 8 - x / 8$ }, { x , 0, 7}]



In[89]:= **Simplify**[**D**[$x / (x^2 + 1)$, x]]

Out[89]=
$$\frac{1 - x^2}{(1 + x^2)^2}$$

In[90]:= **Simplify**[**D**[$x / (x^2 + 1)$, { x , 2}]]

Out[90]=
$$\frac{2 x (-3 + x^2)}{(1 + x^2)^3}$$

In[91]:= **Sqrt**[3] / (**Sqrt**[3]^2 + 1)

Out[91]=
$$\frac{\sqrt{3}}{4}$$

In[97]:= **N**[**Sqrt**[3] / (**Sqrt**[3]^2 + 1), 20]

Out[97]= 0.43301270189221932338