

Sets + Power sets

A	P(A)	A	P(A)
\emptyset	$\{\emptyset\}$	0	1
$\{1\}$	$\{\emptyset, \{1\}\}$	1	2
$\{1, 2\}$	$\{\emptyset, \{1\}, \{2\}, \{1, 2\}\}$	2	4
$\{1, 2, 3\}$	$\{\emptyset, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}\}$	3	8
$\{1, 2, 3, 4\}$	$\{\emptyset, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\},$ $\{4\}, \{1, 4\}, \{2, 4\}, \{3, 4\}, \{1, 2, 4\}, \{1, 3, 4\}, \{2, 3, 4\},$ $\{1, 2, 3, 4\}\}$	4	16
	Inductively, $P(\{1, \dots, n\}) = P(\{1, \dots, n-1\}) \cup \{\{n\} \cup s \mid s \in P(\{1, \dots, n-1\})\}$ has twice as many elements as $P(\{1, \dots, n-1\})$.	n	2^n