

Answer the questions in the spaces provided on the question sheets. If you run out of room for an answer, continue on the back of the page. Circle or box your answers. Show all work.

Name: _____

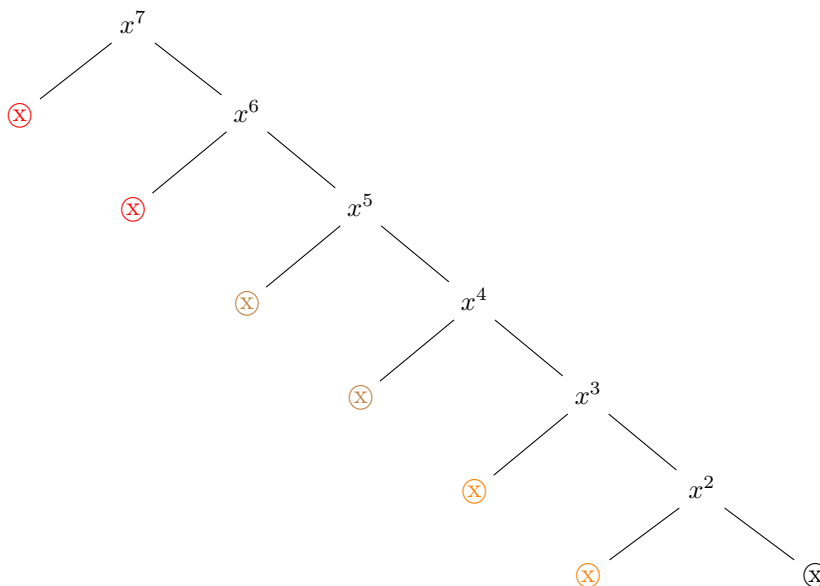
ID number: _____

Question	Points	Score
1	4	
2	4	
3	4	
4	4	
5	4	
6	4	
7	4	
8	4	
9	4	
10	4	
11	4	
12	4	
13	4	
14	4	
15	4	
16	6	
17	6	
18	6	
19	6	
20	6	
21	6	
22	6	
Total:	102	

1. (4 points) Simplify:

$$\sqrt{\frac{x^7}{9}}$$

Solution:



This gives: $\frac{x^3\sqrt{x}}{3}$

2. (4 points) Factor completely: $x^3 + 125$

Solution: I use the Difference of Cubes method and use SOAP. This gives: $(x + 5)(x^2 - 5x + 25)$. I check to see if $(x^2 - 5x + 25)$ can be factored. The quadratic formula gives

$$x = \frac{5 \pm \sqrt{25 - 4(25)}}{2}$$

Under the square root is a negative number, so $x^2 - 5x + 25$ cannot be factored further. This means my final answer is $(x + 5)(x^2 - 5x + 25)$.

3. (4 points) Solve for
- x
- :

$$y = \frac{4x - 7}{2} + B$$

Solution:

$$y - B = \frac{4x - 7}{2}$$

$$2(y - B) = 4x - 7$$

$$2(y - B) + 7 = 4x$$

$$\boxed{\frac{2(y - B) + 7}{4} = x}$$

4. (4 points) Find the complete solution set and write your answer in both interval notation and inequality notation:
- $7 - 5x \leq 47$

Solution:

$$-5x \leq 40$$

$$x \geq -8$$

I check a value in this range. I choose 0:

$$7 - 5(0) \leq 47$$

$$7 \leq 47$$

This answer works so my answer is $\boxed{x \geq -8}$. I convert this to interval notation as $\boxed{[-8, \infty)}$

5. (4 points) Find the complete solution set and write your answer in both interval notation and inequality notation
- $2 < 5 - \frac{x}{4} \leq 27$

Solution:

$$-3 < -\frac{x}{4} \leq 22$$

$$\underline{12 > x \geq -88}$$

I check a value in this range. I choose 0:

$$2 < 5 - \frac{0}{4} \leq 27$$

$$2 < 5 \leq 27$$

This answer works so my answer is $\boxed{12 > x \geq -88}$. I write this in inequality notation as $\boxed{[-88, 12)}$

6. (4 points) Find the distance between $(6, 4)$ and $(10, 7)$

Solution: I use the distance formula with $x_1 = 6$, $y_1 = 4$, $x_2 = 10$, and $y_2 = 7$.

$$d = \sqrt{(10 - 6)^2 + (7 - 4)^2}$$

$$d = \sqrt{4^2 + 3^2}$$

$$d = \sqrt{16 + 9}$$

$$d = \sqrt{25}$$

$$\boxed{d = 5}$$

7. (4 points) Find the midpoint between $(a, 10)$ and $(5a, 6)$.

Solution: I use the Midpoint Formula with $x_1 = a$, $y_1 = 10$, $x_2 = 5a$, $y_2 = 6$. This gives:

$$(x, y) = \left(\frac{a + 5a}{2}, \frac{10 + 6}{2} \right)$$

$$= \left(\frac{6a}{2}, \frac{16}{2} \right)$$

$$= \boxed{(3a, 8)}$$

8. (4 points) If a line AB has endpoint $A = (2, 1)$ and midpoint $M = (12, 3)$, find B .

Solution: I set up two equations using the Midpoint Formula:

$$\frac{2 + x}{2} = 12$$

$$2 + x = 24$$

$$x = 22$$

$$\frac{1 + y}{2} = 3$$

$$1 + y = 6$$

$$y = 5$$

This gives that $\boxed{B = (22, 5)}$.

9. (4 points) What is the x -intercept(s) of the following graph:

x :	1	8	0	3	4
y :	5	0	6	3	2

Solution: The x -intercept(s) are the values when $y = 0$. For this graph, the only x -intercept is at $(8, 0)$.

10. (4 points) Find the y -intercepts of:

$$4y^2 - 10x^2 = 36$$

Solution: To find the y -intercepts I plug in $x = 0$ and get

$$4y^2 - 10(0)^2 = 36$$

$$4y^2 = 36$$

$$y^2 = 9$$

$$y = 3 \text{ and } y = -3$$

Thus my y -intercepts are $(0, 3)$ and $(0, -3)$.

11. (4 points) Find the horizontal line that goes through the point $(31, 25)$

Solution: Points on a horizontal line all have the same y -value. Thus the line is $y = 25$.

12. (4 points) Is the following relation a function? If no, state why.

x :	0	1	2	3	4	5
y :	1	2	3	4	2	5

Solution: There are no two x -values in common, so yes this is a function.

13. (4 points) Is the following relation a function? If no, state why.

$x :$	1	2	3	4	2	5
$y :$	0	1	2	3	4	5

Solution: There are two values of 2 for x that go to different values of y , so this is not a function.

14. (4 points) Find the range of $y = x^2 + 9$

Solution: The range of $y = x^2$ is $[0, \infty)$ so the range of $y = x^2 + 9$ is .

15. (4 points) Find the domain of

$$y = \frac{7}{x^2 + x - 20}$$

Solution: I factor the bottom and get

$$y = \frac{7}{(x-4)(x+5)}$$

so the denominator equals 0 when $x = 4$ and $x = -5$ so my domain is all $x \neq \{4, -5\}$. I write this in interval notation by .

16. (6 points) Simplify:

$$\left(\frac{2x^{-5}y^7}{3x^{-8}y^{-4}} \right)^6$$

Solution:

$$\begin{aligned} &= \frac{2^6 x^{-30} y^{42}}{3^6 x^{-48} y^{-24}} \\ &= \frac{2^6 y^{42} x^{48} y^{24}}{3^6 x^{30}} \\ &= \boxed{\frac{64y^{66}x^{18}}{729}} \end{aligned}$$

17. (6 points) Rationalize the denominator. (You do not need to simplify the numerator):

$$\frac{1 + \sqrt{2}}{4 - 3\sqrt{5}}$$

Solution:

$$\begin{aligned} &= \frac{1 + \sqrt{2}}{4 - 3\sqrt{5}} \cdot \frac{4 + 3\sqrt{5}}{4 + 3\sqrt{5}} \\ &= \frac{(1 + \sqrt{2})(4 + 3\sqrt{5})}{(4 - 3\sqrt{5})(4 + 3\sqrt{5})} \\ &= \frac{(1 + \sqrt{2})(4 + 3\sqrt{5})}{16 - 12\sqrt{5} + 12\sqrt{5} - 9(5)} \\ &= \frac{(1 + \sqrt{2})(4 + 3\sqrt{5})}{16 - 45} \\ &= \frac{(1 + \sqrt{2})(4 + 3\sqrt{5})}{-29} \\ &= \boxed{-\frac{(1 + \sqrt{2})(4 + 3\sqrt{5})}{29}} \end{aligned}$$

18. (6 points) Factor completely:

$$4x^3 - 36x^2 - 9x + 81$$

Solution:

$$\begin{aligned} &= 4x^2(x - 9) - 9(x - 9) \\ &= (4x^2 - 9)(x - 9) \\ &= \boxed{(2x - 3)(2x + 3)(x - 9)} \end{aligned}$$

19. (6 points) Find the complete solution set:

$$\sqrt{4x - 3} = x$$

Solution:

$$\begin{aligned} 4x - 3 &= x^2 \\ x^2 - 4x + 3 &= 0 \\ (x - 3)(x - 1) &= 0 \end{aligned}$$

Thus there are two possible solutions: $\underline{x=3}$ and $\underline{x=1}$. I plug in both answers to the original equation

$$\begin{array}{ll} \sqrt{4(1) - 3} = 1 & \sqrt{4(3) - 3} = 3 \\ \sqrt{4 - 3} = 1 & \sqrt{12 - 3} = 3 \\ \sqrt{1} = 1 & \sqrt{9} = 3 \\ 1 = 1 & 3 = 3 \end{array}$$

Both solutions work, so the answer is $\boxed{x = 3 \text{ and } x = 1}$

20. (6 points) Find the complete solution set:

$$|5x + 8| = x$$

Solution:

$$5x + 8 = x$$

$$4x = -8$$

$$\underline{x = -2}$$

$$-(5x + 8) = x$$

$$-5x - 8 = x$$

$$6x = -8$$

$$\underline{x = -\frac{8}{6}}$$

Now I plug both solutions in to check my answers:

$$|5(-2) + 8| = -2$$

$$|-10 + 8| = -2$$

$$|-2| = -2$$

$$2 = -2$$

$$|5(-\frac{8}{6}) + 8| = -\frac{8}{6}$$

$$|\frac{-40}{6} + \frac{48}{6}| = -\frac{8}{6}$$

$$|\frac{8}{6}| = -\frac{8}{6}$$

$$\frac{8}{6} = -\frac{8}{6}$$

Neither solution works so the final answer is no solution.

21. (6 points) Find the center and radius of $x^2 - 12x + y^2 + 8y - 12 = 0$

Solution: I need to complete the square:

$$x^2 - 12x + 36 + y^2 + 8y + 16 = 12 + 36 + 16$$

$$(x - 6)^2 + (y + 4)^2 = 64$$

Now that I am in standard form for a circle I can read off my center to be (6, -4) and my radius to be 8.

22. (6 points) What (if any) are the symmetries of

$$7y^2x = 1$$

Solution: I first check for x -axis symmetry:

$$\begin{aligned}7(-y)^2x &= 1 \\7y^2x &= 1\end{aligned}$$

This is my original equation, so . Now I check for y -axis symmetry:

$$\begin{aligned}7y^2(-x) &= 1 \\-7y^2x &= 1\end{aligned}$$

This is not the original equation so . Lastly, I check for origin symmetry:

$$\begin{aligned}7(-y)^2(-x) &= 1 \\7y^2(-x) &= 1 \\-7y^2x &= 1\end{aligned}$$

This is not the original equation, so .