

Quiz 1

Name: key

Row: \_\_\_\_\_

1. Give the definition of the definite integral as a limit of Riemann sums. Briefly explain the meaning of the symbols you use.

[10]

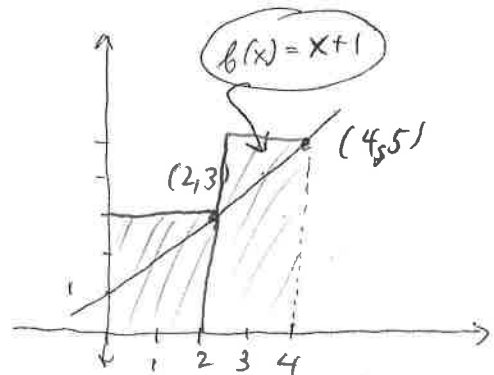
$$\int_a^b f(x) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i^*) \Delta x$$

where  $[a, b]$  is split into  $n$  subintervals, each of length  $\Delta x$ , and  $x_i^*$  is a point in the  $i^{\text{th}}$  subinterval.

[10]

2. Evaluate the Riemann sum for  $f(x) = x + 1$ ,  $0 \leq x \leq 4$ , with two subintervals, taking the sample points to be right endpoints. Show all work.

$$\begin{aligned} R_2 &= f(2) \cdot 2 + f(4) \cdot 2 \\ &= 3 \cdot 2 + 5 \cdot 2 \\ &= 16 \end{aligned}$$



(2 pts off for wrong number of intervals)

(2 pts off for wrong choice of points to evaluate  $f$  at)