Name: _____ Differential Equations, Spring 2017

You must show all your work to receive credit. Calculators are allowed.

Problem 1: (3 points) Consider the second order ODE

$$x'' + \sin(x') + 3te^x = t^3.$$

1. Rewrite as a 2 dim 1st order system. Solution: let $x_1 = x$, $x_2 = x'$ then $x'_2 = x'' = t^3 - \sin(x') - 3te^x = t^3 - \sin(x_2) - 3te^{x_1}$ and the system is $x'_1 = x_2$

$$\begin{array}{rcl} x_1 & = & x_2 \\ x_2' & = & t^3 - \sin(x_2) - 3te^{x_1} \end{array}$$

2. Let \vec{G} be the function such that your answer above is of the form $\vec{x}' = \vec{G}(t, \vec{x})$. Code the function \vec{G} into Matlab. An outline is provided below.

function val=G(t,x)

val=[x(2);t^3-sin(x(2))-3*t*e^(x(1))];