

You must show all your work to receive credit. Calculators are allowed.

Problem 1: (5 points) Find the following derivatives:

$$a) (3x^2 - 2x + 5)' = 6x - 2$$

$$b) \frac{d}{dt}(2^2 + \sqrt{3t}) = \frac{d}{dt}(4 + \sqrt{3} t^{1/2}) = \frac{\sqrt{3}}{2} t^{-1/2}$$

$$c) \frac{d}{dx}[(x+2)^2] = \frac{d}{dx}[x^2 + 4x + 4] = 2x + 4$$

$$d) \left(\frac{2x+1}{x-2}\right)' = \frac{(2x+1)'(x-2) - (2x+1)(x-2)'}{(x-2)^2} = \frac{2(x-2) - (2x+1)(1)}{(x-2)^2} = -\frac{5}{(x-2)^2}$$

$$\begin{aligned} e) [(x^2 + 2x)(x^{-2} + \pi x^{1/3})]' &= (x^2 + 2x)'(x^{-2} + \pi x^{1/3}) + (x^2 + 2x)(x^{-2} + \pi x^{1/3})' \\ &= (2x + 2)(x^{-2} + \pi x^{1/3}) + (x^2 + 2x)(-2x^{-3} + \frac{\pi}{3} x^{-2/3}) \\ &= \frac{7}{3}\pi x^{4/3} - 2x^{-2} + \frac{8}{3}\pi x^{1/3} \end{aligned}$$

Problem 2: (5 points) Use the limit definition of a derivative and properties of limits to prove that $[f(x) + g(x)]' = f'(x) + g'(x)$.

$$\begin{aligned} [f(x) + g(x)]' &= \lim_{h \rightarrow 0} \frac{f(x+h) + g(x+h) - f(x) - g(x)}{h} \\ &= \lim_{h \rightarrow 0} \left[\frac{f(x+h) - f(x)}{h} + \frac{g(x+h) - g(x)}{h} \right] = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} + \lim_{h \rightarrow 0} \frac{g(x+h) - g(x)}{h} \\ &= f'(x) + g'(x) \end{aligned}$$