

Some common list functions

1. Selecting parts of lists

```
head :: [a] -> a    return the first element of a list
tail :: [a] -> [a]  return all but the first element of a non-empty list
last  :: [a] -> a    return the last element of a list
init  :: [a] -> [a]  return all but the last element of a non-empty list
take  :: Int -> [a] -> [a]  return the first n elements of a list
take 5 ( iterate (\x -> x^ 2) 2 ) = [2,4,16,256,65536]
drop  :: Int -> [a] -> [a]  drops the first terms of a list
drop 2 [[5,2,7],[ ],[0,1],[1..3]] = [[0,1],[1,2,3]]
```

2. Getting information about a list

```
length :: [a] -> Int
elem :: Eq a => a -> [a] -> Bool  tell whether the element is a term of the list
elem [ ] [[5,2,7],[ ],[0,1],[1..3]] = True
(!!)  :: [a] -> Int -> a    get the  $n^{th}$  element of a list, where the first element is the
 $0^{th}$ 
[1..10]!!7 = 8
and :: [Bool] -> Bool  logical conjunction
or  :: [Bool] -> Bool  logical disjunction
sum  :: Num a => [a] -> a
product :: Num a => [a] -> a
```

3. Combining lists

```
(++) :: [a] -> [a] -> [a]  join two lists into one
[5,2,7] ++ [0,1] = [5,2,7,0,1]
concat :: [[a]] -> [a]  join list of lists into one
concat [[5,2,7],[ ],[0,1],[1..3]] = [5,2,7,0,1,1,2,3]
zip :: [a] -> [b] -> [(a,b)]  return pairs of corresponding elements of two lists
zip [1..4] "abcdefg" = [(1,'a'),(2,'b'),(3,'c'),(4,'d')]
unzip :: [(a,b)] -> ([a],[b])  reverses the zipping process
unzip [(1,'a'),(2,'b'),(3,'c'),(4,'d')] = ([1,2,3,4],"abcd")
```

4. Creating and manipulating lists

`replicate :: Int -> a -> [a]` make a list of copies of one element

`replicate 3 'Z' = "ZZZ"`

`reverse :: [a] -> [a]` return list in reverse order

`sort :: Ord a => [a] -> [a]` (from the `List` library) return a sorted list

`splitAt :: Int -> [a] -> ([a],[a])` split the list into the first n and the rest

`splitAt 4 "abcdefg" = ("abcd","efg")`

`nub :: Eq a => [a] -> [a]` (from the `List` library) remove duplicates

`nub [1,3,1,4,3,3] = [1,3,4]`

`iterate :: (a -> a) -> a -> [a]` return an infinite list `[x, f(x), f(f(x)), ...]`

`take 5 (iterate (\x -> x^ 2) 2) = [2,4,16,256,65536]`

5. Using functions on lists

`map :: (a -> b) -> [a] -> [b]` apply a function to each term of a list

`map sqrt [1..5] = [1.0, 1.41421, 1.73205, 2.0, 2.23607]`

`filter :: (a -> Bool) -> [a] -> [a]` select elements of a list that satisfy a boolean function

`filter (\x -> length x > 2) [[5,2,7],[],[0,1],[1..3]] = [[5,2,7],[1,2,3]]`

`zipWith :: (a -> b -> c) -> [a] -> [b] -> [c]` zip, then apply a function to each pair

`zipWith (*) [2,3,4] [5,5,0] = [10,15,0]`

`takeWhile :: (a -> Bool) -> [a] -> [a]` returns a list containing elements from the front of the list while the condition is satisfied.

`takeWhile (<1000) (iterate (\x -> 2*x) 2) = [2,4,8,16,32,64,128,256,512]`

`foldr1 :: (a -> a -> a) -> [a] -> a` “fold” the list starting at the right

`foldr1 (-) [1,2,3,4] = (-2)` (calculates $1-(2-(3-4))$)

`foldr :: (a -> b -> b) -> b -> [a] -> b` “fold” the list starting at the right, using a starting value

`foldr (-) 5 [1,2,3,4] = 3` (calculates $1-(2-(3-(4-5)))$)

`foldr (+) 0 = sum`

`foldr (++) [] = concat`

`foldr (&&) True = and`

`foldr ((:).f) [] = map f`

`foldr (\x xs -> if p x then x:xs else xs) [] = filter p`