

Name: \_\_\_\_\_

1. Let  $A = \begin{bmatrix} 9 & 4 \\ -4 & -1 \end{bmatrix}$ . Find the eigenvalues of  $A$ . (6 pts)

2. Let  $A = \begin{bmatrix} 4 & 0 & 1 \\ 0 & 5 & 0 \\ 1 & 0 & 4 \end{bmatrix}$ . One of the eigenvalues of  $A$  is 5. Find a basis for the eigenspace associated with the eigenvalue 5. (7 pts)

3. Let  $A = \begin{bmatrix} 1 & 1 & 1 \\ -1 & 3 & 1 \\ 0 & -3 & 1 \end{bmatrix}$ . For what value (if any) of  $c$  is the vector  $\mathbf{v} = \begin{bmatrix} 2 \\ -1 \\ c \end{bmatrix}$  an eigenvector of  $A$ ? Either find  $c$  and the associated eigenvalue, or explain why no such  $c$  exists. (7 pts)

Bonus: Determine if the following is true or false. Give a proof or counterexample. (5 pts)

If  $A$  has eigenvalue  $\lambda$ , then  $A + A^T$  must have eigenvalue  $2\lambda$ .