Linear Algebra

1. Find the reduced row echelon form of the following matrix. Make sure to specify the row operations that you use. (4 pts)

$$\left[\begin{array}{rrrrr} 0 & 1 & 0 & 1 \\ 1 & -1 & 3 & 0 \\ 0 & 0 & 0 & 2 \end{array}\right]$$

- 2. Find all solutions to each of the following linear systems. Write your answer as a vector. (2 pts each)
  - (a)  $\begin{bmatrix} 1 & 2 & 0 & | & -3 \\ 0 & 1 & -1 & | & 2 \\ 0 & 0 & 1 & | & 3 \end{bmatrix}$ (b)  $\begin{bmatrix} 1 & 0 & 0 & | & 6 \\ 0 & 1 & 0 & | & 2 \\ 0 & 0 & 1 & | & 1 \\ 0 & 0 & 0 & | & 1 \end{bmatrix}$ (c)  $\begin{bmatrix} 1 & 4 & 0 & -2 & | & 1 \\ 0 & 0 & 1 & 0 & | & 3 \\ 0 & 0 & 0 & 0 & | & 0 \end{bmatrix}$