

**Homework 9 :** This homework is due on **November 8**.

1. Find the dimension of the subspace of  $R_5$  consisting of all vectors  $[a \ b \ c \ d \ e]$  of the form  $c = b + 2d$  and  $e = a - b + 4d$ .
2. Find the dimension of the subspace of  $R^4$  spanned by the vectors  $[1 \ 0 \ 0 \ 1]$ ,  $[0 \ 1 \ 0 \ 0]$ ,  $[1 \ 1 \ 1 \ 1]$  and  $[0 \ 1 \ 1 \ 1]$ .
3. Give an example of a 3–dimensional subspace of  $P_3$ .
4. Find the dimension of the subspace of  $M_{44}$  consisting of diagonal matrices.
5. Find the dimension of the subspace of  $M_{33}$  consisting of symmetric matrices.
6. Find the dimension of the subspace of  $P_2$  consisting of all vectors of the form  $at^2 + bt + c$ , where  $b = 2c - 3a$ .
7. Find the dimension of the subspace of the space of all continuous real-valued functions spanned by  $\{\cos^2(t), \sin^2(t), \cos(2t)\}$ .