Class Problem Math 2513 1/27/05

DEFINITION: If  $x = x_1 x_2 x_3 \cdots x_{n-1} x_n$  is a bit string of length n then a **substring of** x is a bit string of the form  $x_i x_{i+1} \cdots x_k$  where i and k are any integers satisfying  $1 \le i \le n$  and  $1 \le k \le n$ . (Note that if k is less than i then we obtain the empty substring.)

PROBLEM. Let  $\alpha$  be the bit string of length 7 given by

$$\alpha = 0011101$$
 .

(a) There are eight different bit strings with length 3. Which (if any) of them do NOT occur as substrings of  $\alpha$ ?

(b) Let A be the set of all substrings of  $\alpha$ . How many elements does A have? List all of the elements of A.