

- i) (10 Points) Let  $y(x) = 3xe^x + 2$ . Find a linear homogeneous constant coefficient differential equation whose solution is  $y(x)$ .

- ii) (10 Points) Consider the differential equation

$$y'' - 4y' + 5y = xe^{2x} \cos(x).$$

Find the appropriate form of a particular solution  $y_p$ , but do not determine the values of the coefficients.

- iii) (5 Points) The roots of the characteristic equation of a constant coefficient homogeneous differential equation are  $2, 2, 0, 0, 3 \pm 5i$ . Find the general solution of this differential equation.